



Simulation study on the avalanche process of the fiber bundles with strong heterogeneities

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ARTICLE INFO

Article history:

Received 27 September 2011

Available online 22 May 2012

Keywords:

Fiber bundle model

Break dynamic

Avalanche process

ABSTRACT

The fiber bundle with strong heterogeneities is an extension of a fiber bundle model based on the classical fiber bundle model to describe the failure process of strongly heterogeneous materials. In order to explore the breaking dynamic properties of strongly heterogeneous materials in short-range correlation, the fiber bundle model with strong heterogeneities in local load redistribution is numerically studied in detail. The impacts of the proportion of two kinds of fibers and the distribution of the failure thresholds on the macroscopic constitutive behavior, the avalanche size distribution and increasing step number of the external load are investigated, respectively. The numerical results show that there is a local plastic plateau in the constitutive curve at a critical proportion of two kinds of fibers. Strong intensity fibers in material can nontrivially increase the intensity and stability of the system by altering the microscopic properties of the failure process.

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1. Introduction

The microscopic mechanism and statistical properties of the rupture of disordered materials have attracted much technological and industrial interest and have been widely studied in statistical physics over the past decades. Due to the inherent nonuniformity and disorder in actual materials, one available theoretical approach to investigate their microscopic properties is the statistical method. The presence of disorder in actual materials introduces remarkable fluctuations based on the statistical properties [1]. Most of the theoretical investigations on the rupture of disordered materials rely on the fiber bundle model (FBM), which involves the main factors in the rupture process. However, the algorithm of FBM is so simple that it is possible to obtain exact results by analytical methods or credible statistical properties through numerical simulation of large systems [2,3]. The FBM consists of a set of parallel fibers having statistically distributed strength. The sample is loaded parallel to the fiber direction and the fibers fail if the load on them exceeds their threshold value. In stress-controlled experiments, after each fiber failure, the load carried by the broken fiber is redistributed among the intact ones.

The subsequent load redistribution after consecutive fiber failures can lead to an entire avalanche of breakages, which can either stop after a certain number of fibers, keeping the integrity of the bundle, or can be catastrophic, resulting in the macroscopic failure of the entire system. Considering the different strengths of transverse association in the rupture process, the type of mechanism by which the extra stress caused by a fiber failure is redistributed among the unbroken fibers can be classed as either global load sharing (GLS) or local load sharing (LLS). The rupture process can be influenced crucially by the type of extra stress redistribution. The simpler case is the GLS models, in which the load previously carried by a failed fiber is shared equally by all the remaining intact fibers in the system. The FBM with GLS is usually the starting point for more complex investigations, since it is possible to obtain the exact analytic solution. Compared to the model with GLS, the

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more realistic case is the model with LLS. A special case of the LLS is the model with a one-dimensional geometry where the two nearest neighbor fibers take up all the extra stress caused by a fiber failure. Due to the local spatial correlations, the analytic treatment of LLS bundles has serious limitations. Most of the studies in this case rely on large-scale computer simulations [4].

The main property of the breakdown process in fiber bundles is the size distribution of the burst avalanches, which is one of the most important characteristics of the microscopic fracture process and can be monitored experimentally by acoustic emission techniques [5–7]. In the GLS limit, the avalanche distributions of fiber bundles with various fracture threshold distributions follow a universal power law with an exponent $-5/2$ [8–10]. In the LLS case, however, the avalanche size distribution is more complex, depending on the specific form of the threshold distributions [11,12].

In order to obtain a more realistic description, especially for the failure of composites, a series of deformation models based on the classical FBM have been introduced. Pradhan et al. [13–15] presented a series of papers to investigate the breakdown of a random fiber bundle model with a lower cutoff in fiber threshold distribution, both in GLS and in LLS. The existence of a crossover behavior near criticality makes it possible to predict the imminent global failure point of the system [16,17]. Raischel et al. [18] studied the failure properties of fiber bundles with a finite lower cutoff of the strength disorder, varying the range of interaction between the limiting cases of GLS and LLS. Computer simulations revealed that, at the interaction local load sharing, the avalanche distribution of the FBM has a more complicated shape. Divakaran and Dutta [19] investigated avalanche size distributions considering the FBM with mixed threshold distributions. The results show that, in the GLS case, the avalanche size distributions obey a universal power law. Some research has also considered the FBM with a continuous damage law, which means that the stiffness of fibers gradually decreases in consecutive failure events before complete rupture [20–23].

Recently, Hidalgo et al. [24] introduced the FBM with strong heterogeneities, based on the classical FBM. The system was assumed to have two components, one of which is characterized by a strength distribution, while the other one is unbreakable. Under the GLS condition, the presence of unbreakable elements has a substantial effect on the fracture process of the system.

In the previous works, Hidalgo et al. considered GLS in the form of load redistribution after a single fiber failure. By comparison, the LLS can better describe the stress redistribution in actual heterogeneous materials, also the method of stress redistribution can have a decisive impact on the fracture process [4]. In order to reveal the deeper properties of the fracture process of strongly heterogeneous materials in short-range correlation, the FBM with strong heterogeneities in LLS, based on Ref. [24], is studied numerically in detail. Specifically, the impacts of the proportion of two kinds of fibers and the distribution of the failure thresholds on the macroscopic constitutive behavior, the critical stress, the maximum avalanche size, the avalanche size distribution, and increasing step number of the external load is investigated. The numerical results show that there is a local plastic plateau in the constitutive curve at a critical proportion of two kinds of fibers. With a small proportion of unbreakable fibers, the overall avalanche size distribution does not satisfy the power-law relationship, only in the limit of large avalanche size will the distribution meet the asymptotic power-law relationship, similar to the one of classical FBM in LLS. When the proportion of unbreakable fibers is large, the whole avalanche size distribution shows approximate power-law behavior.

2. Avalanche process of fiber bundles with strong heterogeneities

The system under consideration is composed of N fibers, with the same Young's modulus $E = 1$, assembled in parallel on a one-dimensional lattice of length L . In order to capture the large variation of disordered material properties, the fiber bundle is assumed to be composed of two subsets of fibers with obviously different breaking characteristics: A fraction α of fibers is strong in the sense that they never break, while fibers of the remaining $1 - \alpha$ fraction are normal and break when the load on them exceeds a threshold value. The disorder of the break threshold is characterized by the probability density p , and the cumulative probability distribution function is

$$P(\sigma) = \int_0^\sigma p(x) dx. \quad (1)$$

In the following simulation it is instructive to consider two different strength distributions for the breakable fibers, namely a uniform distribution between 0 and 1, and a Weibull distribution with the cumulative distribution function

$$P(\sigma) = 1 - \exp[-(\sigma/\lambda)^m] \quad (2)$$

where $m = 2$, $\lambda = 1$ according to extensive research to the FBM. In the simulation, the load is increased quasistatically, i.e. the stress is increased to break only the weakest intact fiber, from which the released stress is shared by the two nearest neighbor fibers. In order to get reliable results, we identify the number of fibers $N = 100\,000$, the following results are the average of 1000 simulations.

To reveal the macroscopic dynamic property in the failure process of the model, the constitutive laws of the model for various fractions α are obtained by numerical simulations. Figs. 1 and 2 correspond to the uniform distribution and the Weibull distribution for the break threshold disorder, respectively. When the value of strain ε is large enough, the normal fibers of fraction $1 - \alpha$ will break completely and the unbreakable fibers of fraction α will take all the stress, so at this time the

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