



ELSEVIER

Contents lists available at ScienceDirect

## Mathematical Social Sciences

journal homepage: [www.elsevier.com/locate/econbase](http://www.elsevier.com/locate/econbase)

# Benchmarking the effective literacy rate

Travis Lee\*

Department of Economics, Cornell University, Ithaca, NY 14853, USA

## ARTICLE INFO

### Article history:

Received 18 June 2007

Received in revised form

5 March 2008

Accepted 10 March 2008

Available online 18 March 2008

### JEL classification:

I2

I3

O15

O2

### Keywords:

Literacy

Education

Inequality

Isolation

## ABSTRACT

Several authors have identified an externality accruing to proximate illiterates, that is, illiterate people with access to a literate person. The standard literacy rate ignores this externality; measures of *effective* literacy are sensitive to it. Nearly all measures of effective literacy appearing in the literature are greater than or equal to  $R$ . In fact, the best known of these, the Basu–Foster measure  $\mathcal{L}^*$ , is strictly greater in virtually every case (see Basu and Foster [Basu, Kaushik, Foster, James, 1998. On measuring literacy. *Economic Journal* 108 (451), 1733–1749]). Although the inequality  $\mathcal{L}^* \geq R$  is an unintended consequence of their construction, it amounts to setting a benchmark for the effective literacy rate. This note examines Basu and Foster's framework and offers an alternative benchmark.

© 2008 Elsevier B.V. All rights reserved.

## 1. Introduction

The standard literacy rate,  $R$ , equal to the number of literate adults as a percentage of the adult population, is a widely used measure of literacy, in spite of the fact that it ignores significant aspects of literacy. In particular, several authors<sup>1</sup> have identified an externality accruing to the illiterate members of households which include at least one literate member, so-called proximate illiterate people. Empirical evidence suggests this externality is large (see Gibson (2001)).

Measures of literacy which are sensitive to the intrahousehold externality are termed measures of *effective* literacy. There is a growing literature on the construction and characterization of such measures, beginning with Basu and Foster (1998). Their measure  $\mathcal{L}^*$  is  $R + \alpha P$ , where  $P$  is the proximate illiteracy rate (percentage of proximate illiterate adults in the adult population) and  $\alpha$  is a real number strictly between zero and one. From this formulation, it is clear that  $\mathcal{L}^*$  is greater than or equal to  $R$ . In

\* Tel.: +1 315 396 4105.

E-mail address: [JTL29@Cornell.edu](mailto:JTL29@Cornell.edu).

<sup>1</sup> See, for example, Green et al. (1985), Basu and Foster (1998), Basu et al. (2000), Gibson (2001) and Maddox (2007).

fact  $\mathcal{L}^* > R$  for any society which includes a proximate illiterate person. This result is a consequence, not an assumption, of their axiomatic approach (more on this observation below), and yet adopting  $\mathcal{L}^*$  to measure literacy amounts to setting a benchmark for the effective literacy rate, namely  $\mathcal{L}^* \geq R$ .

Other authors have extended Basu and Foster’s ideas. Dutta (2004), Subramanian (2004), and Valenti (2002) have given measures for which the extent of the externality depends on the rate of literacy within each household. In almost every case, the proposed measure of literacy is bounded below by the standard literacy rate. Additional authors have offered further extensions (see Basu et al. (2001) and Mitra (2002)), but the problem of benchmarking remains unresolved.

The inequality  $\mathcal{L}^* \geq R$  amounts to taking a particular view of illiteracy, namely that proximate illiteracy is better than illiteracy, as measured by  $R$ . As detailed below, there are other possible points of view. In particular, one may view proximate illiteracy as the normal state of illiteracy; in other words, one expects an illiterate person to have some access to literacy skills through others. This perspective is best captured by a measure of literacy less than or equal to  $R$ . In fact, the benchmark  $\mathcal{L}^* \geq R$  can lead to perplexing results, even when comparing two simple societies, when one has greater literacy and the other greater proximate illiteracy. These examples suggest  $\mathcal{L}^*$  may not adequately measure the trade off between literacy and proximate illiteracy. Improvements can be obtained by considering other measures. Further there is some reason for practical concern, in that  $\mathcal{L}^*$  inflates the standard literacy rate, which may lead to complacency on the part of policymakers or distortion of public policy.

For these reasons, there has been some interest in obtaining new measures of effective literacy,  $\mathcal{L}$ , which are sensitive to the intrahousehold externality but which satisfy the opposite benchmark, that is  $\mathcal{L} \leq R$ . This note offers a new measure and a set of axioms characterizing it. This measure is  $\mathcal{L}' = (1 - \alpha I)R$  for  $0 < \alpha \leq 1$ , where  $I$  is the percentage of isolated illiterate adults (illiterate adults who are not proximate).

Subramanian has already derived the measure of literacy  $(1 - I)R$  from different motivations. Although he does not provide a complete axiomatization, he does give an interesting characterization of  $(1 - I)R$  as a function of  $R$  and a measure of efficiency loss  $I/(1 - R)$  satisfying certain properties. An alternative approach is provided here, and the presence of  $\alpha$  in  $\mathcal{L}' = (1 - \alpha I)R$  may permit empirical comparisons.

Section 2 introduces the Basu–Foster axiomatic framework and their measure  $\mathcal{L}^*$ . This section serves as a starting point for exploring the consistency of their framework with other possible benchmarks. Section 3 concerns the new measure  $\mathcal{L}'$ , and Theorem 1 characterizes  $\mathcal{L}'$  via a set of axioms.

## 2. A critique of the Basu–Foster approach

Denote by  $\Delta$  the set of all societies. A society  $\mathbf{x} \in \Delta$  is a vector of households,  $\mathbf{x} = (\mathbf{x}^1, \dots, \mathbf{x}^{m(\mathbf{x})})$ , where  $m(\mathbf{x})$  is the number of households in  $\mathbf{x}$ . The vector  $x^h = (\mathbf{x}_1^h, \dots, \mathbf{x}_{n(\mathbf{x}^h)}^h)$  denotes the situation of household  $h$ , where  $n(\mathbf{x}^h)$  is the size of household  $h$  and  $x_i^h \in \{0, 1\}$  the situation of individual  $i$  in household  $h$ . The number of individuals in society  $\mathbf{x}$  is denoted  $n(\mathbf{x})$ , so that  $n(\mathbf{x}) = \sum_{h=1}^{m(\mathbf{x})} n(\mathbf{x}^h)$ . Individual  $i$  in household  $h$  is *literate* if  $x_i^h = 1$ ; she is *proximate illiterate* if  $x_i^h = 0$  and there exists  $j$  such that  $x_j^h = 1$ ; she is *isolated illiterate* if  $x_i^h = 0$  and  $x_j^h = 0$ , for all  $j$  in household  $h$ . The number of literate, proximate illiterate, and isolated illiterate individuals in society  $\mathbf{x}$  are denoted as  $r(\mathbf{x})$ ,  $p(\mathbf{x})$ , and  $i(\mathbf{x})$ , so that  $n(\mathbf{x}) = r(\mathbf{x}) + p(\mathbf{x}) + i(\mathbf{x})$ , and the corresponding percentages are  $R(\mathbf{x}) = r(\mathbf{x})/n(\mathbf{x})$ ,  $P(\mathbf{x}) = p(\mathbf{x})/n(\mathbf{x})$ , and  $I(\mathbf{x}) = i(\mathbf{x})/n(\mathbf{x})$ .

Basu and Foster give five axioms which characterize their literacy measure  $\mathcal{L}^*$ . Quoting from Basu and Foster (1998), their axioms are as follows:

**Axiom A (Anonymity).** If  $\mathbf{x} \in \Delta$  is obtained from  $\mathbf{y} \in \Delta$  by either a permutation of households or a permutation of individuals within a household, then  $\mathcal{L}(\mathbf{x}) = \mathcal{L}(\mathbf{y})$ .

Society  $\mathbf{x}$  is obtained from society  $\mathbf{y}$  by a *simple increment* if for some  $(h, j)x_j^h = 1$  and  $y_j^h = 0$ , while  $x_j^{h'} = y_j^{h'}$  for all  $(h', j) \neq (h, j)$ .

**Axiom M (Monotonicity).** If  $\mathbf{x} \in \Delta$  is obtained from  $\mathbf{y} \in \Delta$  by a simple increment, then  $\mathcal{L}(\mathbf{x}) > \mathcal{L}(\mathbf{y})$ .

متن کامل مقاله

دریافت فوری ←

**ISI**Articles

مرجع مقالات تخصصی ایران

- ✓ امکان دانلود نسخه تمام متن مقالات انگلیسی
- ✓ امکان دانلود نسخه ترجمه شده مقالات
- ✓ پذیرش سفارش ترجمه تخصصی
- ✓ امکان جستجو در آرشیو جامعی از صدها موضوع و هزاران مقاله
- ✓ امکان دانلود رایگان ۲ صفحه اول هر مقاله
- ✓ امکان پرداخت اینترنتی با کلیه کارت های عضو شتاب
- ✓ دانلود فوری مقاله پس از پرداخت آنلاین
- ✓ پشتیبانی کامل خرید با بهره مندی از سیستم هوشمند رهگیری سفارشات