



Parallel GRASP with path-relinking for job shop scheduling

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Abstract

In the job shop scheduling problem (JSP), a finite set of jobs is processed on a finite set of machines under certain constraints, such that the maximum completion time of the jobs is minimized. In this paper, we describe a parallel greedy randomized adaptive search procedure (GRASP) with path-relinking for the JSP. Independent and cooperative parallelization strategies are described and implemented. Computational experience on a large set of standard test problems indicates that the parallel GRASP with path-relinking finds good-quality approximate solutions of the JSP.

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1. Introduction

The job shop scheduling problem (JSP) is a well-studied problem in combinatorial optimization. It consists in processing a finite set of jobs on a finite set of machines. Each job is required to complete a set of operations in a fixed order. Each operation is processed on a specific machine for a fixed duration. Each machine can process at most one job at a time and once a job initiates processing on a given machine it must

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complete processing on that machine without interruption. A schedule is a mapping of operations to time slots on the machines. The makespan is the maximum completion time of the jobs. The objective of the JSP is to find a schedule that minimizes the makespan.

Mathematically, the JSP can be stated as follows. Given a set \mathcal{M} of machines (where we denote the size of \mathcal{M} by $|\mathcal{M}|$) and a set \mathcal{J} of jobs (where the size of \mathcal{J} is denoted by $|\mathcal{J}|$), let $\sigma_1^j \prec \sigma_2^j \prec \dots \prec \sigma_{|\mathcal{M}|}^j$ be the ordered set of $|\mathcal{M}|$ operations of job j , where $\sigma_k^j \prec \sigma_{k+1}^j$ indicates that operation σ_{k+1}^j can only start processing after the completion of operation σ_k^j . Let \mathcal{O} be the set of operations. Each operation σ_k^j is defined by two parameters: \mathcal{M}_k^j is the machine on which σ_k^j is processed and $p_k^j = p(\sigma_k^j)$ is the processing time of operation σ_k^j . Defining $t(\sigma_k^j)$ to be the starting time of the k th operation $\sigma_k^j \in \mathcal{O}$, the JSP can be formulated as follows:

$$\begin{aligned} & \text{minimize} && C_{\max} \\ & \text{subject to} && C_{\max} \geq t(\sigma_k^j) + p(\sigma_k^j) \quad \forall \sigma_k^j \in \mathcal{O}, \\ & && t(\sigma_k^j) \geq t(\sigma_l^j) + p(\sigma_l^j) \quad \forall \sigma_l^j \prec \sigma_k^j, & (1a) \\ & && t(\sigma_k^j) \geq t(\sigma_l^j) + p(\sigma_l^j) \vee & (1b) \\ & && t(\sigma_l^j) \geq t(\sigma_k^j) + p(\sigma_k^j) \quad \forall \sigma_l^j, \sigma_k^j \in \mathcal{O} \text{ such that } \mathcal{M}_{\sigma_l^j} = \mathcal{M}_{\sigma_k^j}, \\ & && t(\sigma_k^j) \geq 0 \quad \forall \sigma_k^j \in \mathcal{O}, \end{aligned}$$

where C_{\max} is the makespan to be minimized.

A feasible solution of the JSP can be built from a permutation of \mathcal{J} on each of the machines in \mathcal{M} , observing the precedence constraints, the restriction that a machine can process only one operation at a time, and requiring that once started, processing of an operation must be uninterrupted until its completion. Once the permutation of \mathcal{J} is given, its feasibility status can be determined in $O(|\mathcal{J}| \cdot |\mathcal{M}|)$ time. The feasibility-checking procedure determines the makespan C_{\max} for feasible schedules [1]. Since, each set of feasible permutations has a corresponding schedule, the objective of the JSP is to find, among the feasible permutations, the one with the smallest makespan.

The JSP is NP-hard [2] and has also proven to be computationally challenging. Exact methods [3–7] have been successful in solving small instances, including the notorious 10×10 instance of Fisher and Thompson [8], proposed in 1963 and only solved 20 years later. Problems of dimension 15×15 are still considered to be beyond the reach of today's exact methods. For such problems there is a need for good heuristics. Surveys of heuristic methods for the JSP are given in [9,10]. These include dispatching rules reviewed in [11], the shifting bottleneck approach [3,12], local search [10,13,14], simulated annealing [13,15], tabu search [1,14,16], and genetic algorithms [17]. Recently, Binato et al. [18] described a greedy randomized adaptive search procedure (GRASP) for the JSP. A comprehensive survey of job shop scheduling techniques can be found in Jain and Meeran [19]. In this paper, we present a new parallel GRASP with path-relinking for the JSP.

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