



# The economic production quantity with rework process in supply chain management

Kun-Jen Chung\*

College of Business, Chung Yuan Christian University, 32023 Chung Li, Taiwan, ROC

## ARTICLE INFO

### Article history:

Received 18 June 2010

Accepted 10 July 2011

### Keywords:

Economic order quantity

Economic production

Rework process and planned backorders

## ABSTRACT

Cardenas-Barron [L.E. Cardenas-Barron, Economic production quantity with rework process at a single-stage manufacturing system with planned backorders, Computers and Industrial Engineering 57 (2009) 1105–1113] minimizes the annual total relevant cost  $TC(Q, B)$  to find the economic production quantity with rework process at a manufacturing system and assumes that  $TC(Q, B)$  is convex. So, the solution  $(\bar{Q}, \bar{B})$  satisfying the first-order-derivative condition for  $TC(Q, B)$  will be the optimal solution. However, this paper indicates that  $(\bar{Q}, \bar{B})$  does not necessarily exist although  $TC(Q, B)$  is convex. Consequently, the main purpose of this paper is two-fold:

- (A) This paper tries to develop the sufficient and necessary condition for the existence of the solution  $(\bar{Q}, \bar{B})$  satisfying the first-derivative condition of  $TC(Q, B)$ .
- (B) This paper tries to present a concrete solution procedure to find the optimal solution of  $TC(Q, B)$ .

© 2011 Elsevier Ltd. All rights reserved.

## 1. Introduction

Cardenas-Barron [1] minimizes the annual total relevant function  $TC(Q, B)$  to find the economic production quantity with rework process at a manufacturing system with planned backorders and assumes that the annual total relevant cost  $TC(Q, B)$  is convex. So, the solution  $(\bar{Q}, \bar{B})$  satisfying the first-derivative condition for  $TC(Q, B)$  will be the optimal solution. However, this paper indicates that  $(\bar{Q}, \bar{B})$  does not necessarily exist although  $TC(Q, B)$  is convex. Consequently, the main purpose of this paper is two-fold:

- (A) This paper tries to develop the sufficient and necessary condition for the existence of the solution  $(\bar{Q}, \bar{B})$  satisfying the first-derivative condition of  $TC(Q, B)$ .
- (B) This paper tries to present a concrete solution procedure to find the optimal solution of  $TC(Q, B)$ .

## 2. The model

The model makes the following assumptions and notations that are used throughout this paper:

Assumptions:

- (1) demand rate is constant and known over horizon planning;
- (2) production rate is constant and known over horizon planning;
- (3) the production rate is greater than demand rate;
- (4) the production of defective products is known;

\* Fax: +886 3 2655099.

E-mail address: [kjchung@cycu.edu.tw](mailto:kjchung@cycu.edu.tw).

### Notations

$D$	Demand rate, units per time
$P$	Production rate, units per time ( $P > D$ )
$R$	Proportion of defective products in each cycle ( $0 < R < 1 - \frac{D}{P}$ )
$K$	Cost of a production setup (fixed cost), \$ per setup
$C$	Manufacturing cost of a product, \$ per unit
$H$	Inventory carrying cost per product per unit of time, $H = iC$
$i$	Inventory carrying cost rate, a percentage
$W$	Backorder cost per product per unit of time (linear backorder cost)
$F$	Backorder cost per product (fixed backorder cost)
$Q$	Batch size (units)
$B$	Size of backorders (units)
$A$	$1 - R$
$E$	$1 - R - \frac{D}{P}$
$L$	$1 - (1 + R + R^2)\frac{D}{P}$
$T$	Time between production runs
$TC(Q, B)$	Total cost per unit of time
$Q^*, B^*$	The optimal solution of $TC(Q, B)$ .

- (5) the products are 100% screened and the screening cost is not considered;
- (6) all defective products are reworked and converted into good quality products;
- (7) scrap is not generated at any cycle;
- (8) inventory holding costs are based on the average inventory;
- (9) backorders are allowed and all backorders are satisfied;
- (10) production and reworking are done in the same manufacturing system at the same production rate;
- (11) two types of backorder costs are considered: linear backorder cost (backorder cost is applied to average backorders) and fixed backorder cost (backorder cost is applied to maximum backorder level allowed);
- (12) inventory storage space and the availability of capital is unlimited;
- (13) the model is for only one product;
- (14) the planning horizon is infinite.

Based on the above assumptions and notation, Cardenas-Barron [1] show that the total cost per unit of time  $TC(Q, B)$  can be written as:

$$TC(Q, B) = \frac{KD}{Q} + \frac{HQL}{2} + \frac{HB^2A}{2QE} - HB + \frac{FBD}{Q} + \frac{WB^2A}{2QE} + CD(1 + R). \quad (1)$$

Eq. (1) shows that the respective partial derivatives with respect to  $Q$  and  $B$  can be expressed as:

$$\frac{\partial TC(Q, B)}{\partial Q} = -\frac{KD}{Q^2} + \frac{HL}{2} - \frac{HB^2A}{2Q^2E} - \frac{FBD}{Q^2} - \frac{WB^2A}{2Q^2E}, \quad (2)$$

$$\frac{\partial TC(Q, B)}{\partial B} = \frac{HBA}{QE} - H + \frac{FD}{Q} - \frac{WBA}{QE}. \quad (3)$$

Consider the first-order-derivative condition for  $TC(Q, B)$

$$\frac{\partial TC(Q, B)}{\partial Q} = 0 \quad (4)$$

and

$$\frac{\partial TC(Q, B)}{\partial B} = 0. \quad (5)$$

Eqs. (4) and (5) imply

$$H[AL(H + W) - EH]Q^2 = 2KDA(H + W) - E(FD)^2, \quad (6)$$

$$A(H + W)B = E(HQ - FD). \quad (7)$$

### 3. The sufficient and necessary condition for the existence of the solution of the simultaneous Eqs. (4) and (5)

Let  $(\bar{Q}, \bar{B})$  denote the solution of the simultaneous Eqs. (4) and (5).

متن کامل مقاله

دریافت فوری ←

**ISI**Articles

مرجع مقالات تخصصی ایران

- ✓ امکان دانلود نسخه تمام متن مقالات انگلیسی
- ✓ امکان دانلود نسخه ترجمه شده مقالات
- ✓ پذیرش سفارش ترجمه تخصصی
- ✓ امکان جستجو در آرشیو جامعی از صدها موضوع و هزاران مقاله
- ✓ امکان دانلود رایگان ۲ صفحه اول هر مقاله
- ✓ امکان پرداخت اینترنتی با کلیه کارت های عضو شتاب
- ✓ دانلود فوری مقاله پس از پرداخت آنلاین
- ✓ پشتیبانی کامل خرید با بهره مندی از سیستم هوشمند رهگیری سفارشات