



Comparing models for lot-sizing and scheduling of single-stage continuous processes: Operations research and process systems engineering approaches

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ABSTRACT

In the last years, several researchers from two different academic communities, the Operations Research and the Process Systems Engineering, have been developing mathematical formulations for the lot-sizing and scheduling of single-stage continuous processes with complex setup structures. This problem has been intensively studied due to its importance to a wide range of industries where a single-stage approach is suitable for production planning. This is the case of the glass container, beer, and dairy production. Recent works have been performed by both mentioned communities, however, no intense communication between these research efforts has been observed. This work attempts a systematic analysis on recent formulation developments of both communities. Based on the result of this comparison, a reformulation is proposed that outperforms in the majority of the cases the previous existent formulations for a set of systematically generated random instances.

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1. Introduction

In recent years, it has been verified an efficiency increase associated with both standard mixed-integer linear programming (MIP) solvers and hybrid heuristic methods, creating advantages on the use of mathematical formulations to solve industrial problems (Belvaux & Wolsey, 2001). Moreover, mathematical programming approaches can be more flexible than tailored heuristics to accommodate different problem characteristics that change from industry to industry and from time to time. This context creates the motivation to compare, through exact procedures, formulations that can tackle a very practical problem arising in the industrial production scheduling. This is the case of the lot-sizing and scheduling problem that is widely found in the fast moving consumer goods industry characterized by production systems involving tight capacities and complex setup structures. As an example there is the dairy products production, such as yoghurt. In the production of this good, sequence dependent setup times and/or costs are natural, since for instance changing from producing plain yoghurt to chocolate flavor yields a much smaller setup than the inverse operation. Furthermore, if the company produces the same product for different countries, it then incurs in minor setups while changing between

labels on the same flavor, favoring a product family arrangement. Finally, these industries usually work on a continuous basis, and therefore, setup carry-over has a high impact on the final solution. The sequence dependent setups feature forces the simultaneous decision on sizing and scheduling of the lots, because using an hierarchical decision procedure may induce operational infeasibilities due to lack of capacity (Almada-Lobo, Klabjan, Carravilla, & Oliveira, 2007).

This problem has been receiving an increasing attention from two research communities: the Process Systems Engineering (PSE) and the Operations Research (OR). PSE has been focused more on problems such as the batch scheduling and planning of production systems based on network topologies. Most of the approaches use state-task network (STN) (Kondili, Pantelides, & Sargent, 1993) or resource-task network (RTN) (Pantelides, 1994), with different time representations. On the other hand, the OR has been developing efforts on the definition of the solution convex hull of very structured production problems (e.g. Wolsey, 2002), understanding the advantages of different formulation approaches (e.g. Fleischmann & Meyr, 1997) and developing and benchmarking different heuristic solution methods (e.g. Almada-Lobo & James, 2010). From a scientific publication point of view, the research conducted by both communities has been published in different research journals. Some of the Journals most used by the PSE community are the *Computers and Chemical Engineering* and the *Industrial Engineering and Chemistry Research*, whilst the OR

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research community prefer Journals, such as the *European Journal of Operations Research*, the *Computers and Operations Research* or the *OR Spectrum*. Despite this publishing behavior, the existent boundaries are sometimes crossed (e.g. Stefansson, Sigmarsson, Jensson, & Shah, 2011).

In the OR community the formulations related to lot-sizing and scheduling problems are clustered in *big* and *small bucket* formulations (Karimi, Fatemi Ghomi, & Wilson, 2003). The *big bucket* formulations allow for multiple product setups in a single period, while the *small bucket* formulations allow for at most one setup in each period (cf. Drexel & Haase, 1995). In the PSE community the sequential processes, as the one under study, are essentially modelled with continuous time formulations and event points representation, which may use either *time slots* or *precedence-based* approaches (cf. Mendez, Cerda, Grossmann, Harjunjoski, & Fahl, 2006).

Despite the apparent differences among the two communities, a linkage can be made between both used classifications. In the *big bucket* OR formulations, if sequence dependent setups are to be taken into account, changeover variables are usually used to express consecutive precedence within each period, aspect that has been quite explored within the PSE community. Thus a *precedence-based* approach is inherent to *big bucket* formulations tackling sequence dependent setups. On the other hand, the *time slots* event representation, which is often present in the PSE works, is related to the *general lot-sizing and scheduling problem* (Fleischmann & Meyr, 1997) that may be seen in the OR community as a *small bucket* formulation. This formulation relies on a hybrid time representation with two grids: discrete and continuous. The discrete time grid accounts for external events, such as demand occurrences, whilst the continuous one accounts for the lot-sizing and production sequencing. Within each discrete time period the number of slots is defined as a parameter. This happens to be also the case in the *time slot* formulations, used by the PSE community.

The first aim of this work is to compare and analyze the performance of some existent and well identified formulations, published by the OR and the PSE communities that deal to the operational production planning problem involving lot-sizing and scheduling decisions where a complex setup structure is present. Namely, sequence dependent changeovers, setup families and setup carry-over are considered. The models are solved by a state-of-art MIP solver, and are evaluated by the quality of the upper-bound and of the integrality gap at the end of the run. The choice of the formulations to be compared is arguable. However, it was based on two criteria decided by the authors: the recency of the publications and the usage of the same formulation by different authors. The second aim of this work stems from the comparison and consists of testing a reformulation against the formulation that performs the best on the first computational experiments.

The remainder of this paper is organized as follows. In Section 2 the literature review is outlined and the problem definition is given in Section 3. In Section 4, four formulations are presented and compared, two published by the OR community and two by the PSE community. The *big bucket* formulation proposed by the OR is compared with the *precedence-based* formulation from the PSE in the first subsection. In the second subsection the other two formulations are assessed, namely the *small bucket* from OR and the *time slot* from PSE. In order to perform this comparison some adaptations were made in the original formulations of both communities. This work focuses on the well-known general lot-sizing and scheduling problem (*small bucket*) and capacitated lot-sizing and scheduling problem (*big bucket*) from the OR community. With regard to the PSE community formulations, as they are less standardized, two recent formulations were chosen that were proposed by Erdirlik-Dogan and Grossmann (2008) and Kopanos,

Puigjaner, and Maravelias (2011). These formulations are related to *time slot* and *precedence-based* formulations, respectively. Computational experiments on a set of systematically generated random instances of the formulations are provided in Section 5 and the reformulation is presented and tested in Section 6. Finally, some conclusions and directions for future research are drawn in Section 7.

2. Literature review

The literature on the simultaneous lot-sizing and scheduling problem is extensive. Judging by the number of reviews in this field there is a considerable body of research on this topic (Buschkuhl, Sahling, Helber, & Tempelmeier, 2008; Drexel & Kimms, 1997; Floudas & Lin, 2004; Jans & Degraeve, 2008; Karimi et al., 2003; Mendez et al., 2006; Zhu & Wilhelm, 2006). These reviews present the main features, strengths and limitations of existing modeling and optimization approaches. One of the findings is that manuscripts regarding parallel machines accounting for sequence dependent setup time and cost are just a few and need further developments. The problem considered in this study is within this scope (cf. Section 3). The aim of this review is to illustrate the main trends identified in the OR and the PSE communities. For a complete review on lot-sizing and scheduling models the readers are referred to the aforementioned reviews.

In the OR community, Kang, Malik, and Thomas (1999) formulated this problem with a *big bucket* model using not only the traditional objective function of minimizing the sum of the setup and holding costs, but also accounting for the sales revenue. The authors do not allow for backlogging, hence demand has to be satisfied in each period. To solve this problem a column generation approach is used incorporating a branch-and-bound heuristic. Some years later, Meyr (2002) generalized the previous formulation and included the possibility for sequence dependent setup times and not just setup costs. This *small bucket* formulation is the extension of the general lot-sizing and scheduling problem (Fleischmann & Meyr, 1997) to multiple machines. With a more practical orientation, Günther, Grunow, and Neuhaus (2006) applied the concept of block planning in the production planning and scheduling of a major producer of hair dyes. This concept is very suitable to the make-and-pack industries as it is based on a pre-defined sequence of production orders of variable size. More recently, Almada-Lobo et al. (2007) focused on the extension of the structured capacitated lot-sizing and scheduling problem, which is one of the most used *big bucket* formulations, to include sequence dependent setup costs and times. Kovács, Brown, and Tarim (2009) proposed a new *big bucket* formulation based on the sequences within each period. In a pre-processing step efficient sequences for each period are calculated and this is the starting point for the MIP formulation. This idea was explored by Haase and Kimms (2000) in a previous work, which took advantage of problem specific characteristics to unveil efficient scheduling paths in each period. After finding the right sequence for each period, the only decisions left are related to production quantities. Based on these findings, a tailor-made branch-and-bound is developed and industry case studies are solved. More recently, researchers have focused on the introduction of different features into the classical problems. Menezes, Clark, and Almada-Lobo (2010) focused on the fact that sequence dependent times and costs often do not respect the triangular inequality. Hence, the authors presented a MIP model for the capacitated lot-sizing and scheduling problem allowing for sequence sub-tours and setup crossovers. Inspired in the textile industry, Camargo, Toledo, and Almada-Lobo (2012) proposed three novel mathematical models for the two-stage lot-sizing and scheduling problem. The first stage is continuous whereas the second has features belonging to

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