

An economic order quantity model with defective items and shortages

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Abstract

The fundamental assumption of an economic order quantity (EOQ) model is that 100% of items in an ordered lot are perfect. This assumption is not always pertinent for production processes because of process deterioration or other factors. This paper develops an EOQ model for that each ordered lot contains some defective items and shortages backordered. It is assumed that 100% of each lot are screened to separate good and defective items which are collection of imperfect quality and scrap items. The effect of percentage defective on optimal solution is studied while numerical examples are provided for the developed model.

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1. Introduction

Economic order quantity model (EOQ) is a technique to find out optimum order quantity generally by considering costs of procurement, inventory holding, and backorder. The basic assumption of the classical EOQ model is that 100% of ordered items are perfect. This assumption may not be valid for most of the production environments. Starting from this point, researchers have developed different EOQ and economic production quantity (EPQ) models with percentage defective items.

Rosenblatt and Lee (1986) proposed an EPQ model for a production system which contains defective production. The basic assumption in their model is that the production system produces 100% non-defective products from the starting point of production until a time point which is a random variable. At this time point, system becomes out of control and starts to produce defective items with a percentage of production until end of the production period. It is assumed that the distribution of time passes until system becomes out of control state is exponential. Backorder is not allowed in their model. Kim and Hong (1999) extended Rosenblatt and Lee's (1986) model with the assumption of the distribution of the time passes until system becomes out of control is arbitrarily distributed. Chung and Hou (2003) combined aforementioned models by allowing assumption of

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Nomenclature			
D	demand rate in units per unit time	h	holding cost per unit per unit time
y	order size for each cycle	π	backorder cost per unit per unit time
w	maximum backorder level allowed	θ	percentage of scrap items in defective items
k	fixed cost of placing an order	x	screening rate in units per unit time
c	unit variable cost	d	unit screening cost
p	percentage of defective items in y	$E(\cdot)$	expected value operator
$f(p)$	probability density function of p	t_1	time to build up a backorder level of ‘ w ’ units
s	unit selling price of good-quality items	t_2	time to eliminate the backorder level of ‘ w ’ units
v	unit selling price of imperfect-quality items, $v < c$	t_3	time to screen y units ordered per cycle
c_S	unit disposal cost for scrap items	t	cycle length

backorders. Also, all of these models did not consider the time required to rework on defective items to make them good-quality items.

Hayek and Salameh (2001) developed an EPQ model for percentage defective that has a uniform distribution. The basic assumptions of this model are allowing backorders, all of the defective items are reworked and become perfect quality and rework time also is considered in the model. Chiu (2003) extended Hayek and Salameh’s (2001) model by combining the assumptions of a portion of the defective items are reworked to make them good-quality item instead of reworking on all of the defective items and the remaining items are sold on a sale price.

Chan et al. (2003) developed three EPQ models with the assumption of the quantifiable basic property of produced products has a Gaussian distribution. They classified products as good quality, good quality after reworking, imperfect quality and scrap. Crucial assumptions of these models are not allowing backorders, reworking time is zero and imperfect-quality products are sold on sale prices. The basic assumption which distinguishes these models is selling times of imperfect-quality items are different from each other. Therefore, holding costs per cycle are not identical. Salameh and Jaber (2000) developed an EOQ model for circumstances where a fraction of the ordered lot is of imperfect quality and has a uniform distribution. Their model assumed that shortages are not permitted to occur. Goyal and Cardenas-Barron (2002) reworked on the paper by Salameh and Jaber (2000) and presented a practical approach to find out the optimal lot size. Papachristos and Konstantaras (2006) re-studied and developed the

sufficient conditions for models given by Salameh and Jaber (2000) and Chan et al. (2003).

In many real-life conditions, stockout is unavoidable because of various uncertainties in the related system. Therefore, the occurrence of shortages in inventory could be considered as a natural phenomenon. In this paper, Salameh and Jaber’s (2000) model is extended by allowing shortages back-ordered. Also, the effects of different levels of defectives fractions on lot size and expected total profit are examined.

2. Mathematical model

In this paper, we assumed that a lot size of ‘ y ’ is replenished instantaneously at the beginning of each period with a purchasing price of ‘ c ’ per unit and ordering cost of ‘ k ’ per order. It is assumed that each lot contains percentage defectives of ‘ p ’, with a known probability density function, $f(p)$. Each lot received is screened 100% with a screening rate per unit time of x to separate good and defective items. It is assumed that defective items contain imperfect-quality items with a rate of $1-\theta$ and scrap items with a rate of θ . At the end of screening process, imperfect-quality items are sold as a single lot and scrap items are subtracted from inventory with unit cost of c_S . The selling prices of good- and imperfect-quality items are s and v per unit, respectively, where $s > v$.

The behaviour of the inventory level is illustrated in Fig. 1. It is assumed that the rate of good-quality items which are screened during t_2 is $(1-p)$ in Fig. 1. A part of these good-quality items meet the demand with a rate of D and the remaining is used to eliminate backorders with a rate of

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