



# Cost-optimization heuristic algorithm in safety engineering

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## Abstract

A hierarchical fault tree, on the basis of the system branch tree, is considered. Each basic element at the bottom level may relate to a set of possible primary failures, some of which, in turn, may have an essential influence on critical failures at the top level. We suggest several optimization models with cost objectives which enable diminishing the probability of a critical failure via reducing the probabilities of primary failures to occur. The objective to be minimized is the entire cost of required technical alterations, subject to the pre-given upper permissible level of the critical failure's probability.

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## 1. Introduction

A hierarchical technical system which in the course of its functioning can be the source of large-scale accidents, e.g. nuclear power facilities, is considered. In the last four decades a large number of scientists (see, e.g. Barlow and Lambert, 1975; Fussell, 1975; Golenko-Ginzburg and Papic, 1998; Haasl, 1981; Schneeweiss, 1985; Weber, 1982; Young, 1975, etc.) undertook extensive research in the area of *fault tree analysis* (FTA) in order to develop effective techniques to predict and to prevent various failures of high risk safety technology. Fault tree analysis is mainly based on simulation models, and it can be well-recognized via simulation (Barlow and Lambert, 1975; Ben-Yair, 2001; Golenko-Ginzburg and Gonik, 1998a, b; Golenko-Ginzburg and Gonik, 2002; Golenko-Ginzburg and Papic, 1998; Fussell, 1975) that the probability of a critical failure  $P_{cr}$  at the top level depends mainly on certain primary failures' probabilities at the bottom level. Thus, increasing the reliability of the corresponding elements at the bottom level results in increasing the overall system's technical reliability. Note that most primary failure probabilities can be decreased by introducing corresponding technical alterations which require the lay out of expenditure. The latter may be calculated in advance, either by using experts, or on the basis of statistical analysis of similar technical systems.

Since the required budget to undertake technical alterations and refinements is usually restricted, various trade-off problems of "cost-reliability" type become highly important. However, despite the prevalence of

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FTA, publications on cost-optimization problems in Safety Engineering within the last decades are very scanty (see, e.g. Kuo and Prasad, 2000). They practically do not cover cases of complicated hierarchical technical systems with primary failures at the lower levels and top critical failures at the upper level. Few publications on reliability optimization problems with cost parameters for large-scale systems boil down to the study of various network communications problems (Li and Haimes, 1992), as well as problems of determining optimal levels of component reliabilities and redundancies with respect to multiple objectives (Sakawa, 1981). The results obtained in the area of cost-reliability models for stochastic projects (Golenko-Ginzburg and Gonik, 1998a, b; Golenko-Ginzburg and Gonik, 2002), cannot be applied to engineering systems with hierarchical structure, as well as to hierarchical fault trees.

Consider, that all primary failures at the system's bottom level are enumerated by  $F_\xi$ ,  $1 \leq \xi \leq Q$ . Denote the corresponding primary failure probability by  $P_\xi$ . Assume that, by introducing possible technical improvements, value  $P_\xi$  can be decreased but cannot become less than its lower bound  $P_{\xi \min}$  which is usually obtained by using expert systems.

Determine the corresponding "probability step"  $\Delta P_\xi$ , i.e., a constant reduction, in order to undertake a whole number of steps to reduce the probability of primary failure  $F_\xi$  from  $P_\xi$  to  $P_{\xi \min}$ . Denote the corresponding number of steps by  $N_\xi$ . Thus, relation  $N_\xi \cdot (\Delta P_\xi) = P_\xi - P_{\xi \min}$  holds. Introducing technical improvements to diminish the primary failure probability by one step requires cost expenditures which are pre-given as well. Denote a top critical failure by  $F_{cr}$  with its corresponding probability  $P_{cr}$ . Assume that value  $P_{cr}$  is high enough and has to be reduced in order not to exceed the prescribed upper level  $P_{cr}^*$ . The newly developed cost-optimization problem (the direct problem) is to determine improved primary failures probabilities  $P_{\xi f_\xi}$  of  $F_\xi$  after undertaking  $f_\xi$  consecutive steps ( $f_\xi$  being the step index),  $1 \leq \xi \leq Q$ ,  $0 \leq f_\xi \leq N_\xi$ , which require the minimal accumulated costs to undertake all technical improvements, subject to reliability constraint, i.e., the top level critical probability not to exceed the pre-given upper level  $P_{cr}^*$ . Another cost-optimization problem—the dual one—centers on minimizing the failure probability subject to the cost constraint, i.e., to the restricted budget to carry out the technical improvements.

Both problems have been solved by using a heuristic cost-optimization algorithm via simulation. A numerical example to check the fitness of the algorithm is presented.

## 2. Notation

Let us introduce the following terms:

FT	the fault tree comprising $n$ hierarchical levels with its logical and probabilistic structure (Barlow and Lambert, 1975; Ben-Yair, 2001; Golenko-Ginzburg and Gonik, 1998a, b; Golenko-Ginzburg and Gonik, 2002; Golenko-Ginzburg and Papić, 1998; Fussell, 1975), which enables calculating top critical failure probabilities on the basis of primary failure probabilities;
SM	the simulation model with incoming primary failures at the bottom level and outcome top level failures;
$F_\xi$	primary failure, $1 \leq \xi \leq Q$ ( $Q$ —number of primary failures);
$P_\xi$	the probability of $F_\xi$ (pre-given);
$P_{\xi \min}$	the minimal possible probability value $P_\xi$ which, due to technical conditions, cannot be diminished (pre-given);
$C(P_\xi, P_{\xi \min})$	the cost of technical improvements in order to reduce the primary failure $F_\xi$ by diminishing its probability up to $P_{\xi \min}$ (pre-given);
$\Delta P_\xi$	the "probability step" for value $P_\xi$ in order to implement a technical improvement and diminish value $P_\xi$ by $\Delta P_\xi$ (pre-given);

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